

Forecasting probabilistic seismic shaking for greater Tokyo from 400 years of intensity observations

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The long recorded history of earthquakes in Japan affords an opportunity to forecast seismic shaking exclusively from past shaking. We calculate the time-averaged (Poisson) probability of severe shaking by using more than 10,000 intensity observations recorded since AD 1600 in a 350-km-wide box centered on Tokyo. Unlike other hazard assessment methods, source and site effects are included without modeling, and we do not need to know the size or location of any earthquake or the location and slip rate of any fault. The two key assumptions are that the slope of the observed frequency-intensity relation at every site is the same; and that the 400-year record is long enough to encompass the full range of seismic behavior. Tests we conduct here suggest that both assumptions are sound. The resulting 30-year probability of $I_{JMA} \geq 6$ shaking ($\sim \text{PGA} \geq 0.9$ g or $\text{MMI} \geq \text{IX}$) is 30-40% in Tokyo, Kawasaki, and Yokohama, and 10-15% in Chiba and Tsukuba. This result means that there is a 30% chance that 4 million people will be subjected to $I_{JMA} \geq 6$ shaking during an average 30-year period. We also produce exceedance maps of peak ground acceleration for building code regulations, and calculate short-term hazard associated with a hypothetical catastrophe bond. Our results resemble an independent assessment developed from conventional seismic hazard analysis for greater Tokyo.

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INTRODUCTION

Our goal is to conduct a probabilistic seismic hazard assessment that is driven to the greatest extent possible by observations, and is as free of modeling assumptions as possible. Such an approach is best suited to regions where the record of earthquake shaking is long, the reporting of the shaking is reliable and consistent through time, and possibly where the earthquake rate is high. Fortunately, the great seismologist Tatsuo Usami gathered and codified the historical record of earthquake effects in Japan as his life's work. In addition, studies by *Utsu* [1979], *Takemura* [2003], *Hamada et al.* [2001], and *JMA* [2004] greatly enhanced this trove of data for more recent periods. We digitized, combined, and analyzed these data (Table 1).

Table 1. Sources of intensity data used in this study

Time Period	Data source	Number of $I_{JMA} \geq 3$ observations
1600 - 1884	<i>Usami</i> (1994)	1579
1885 - 1922	<i>Utsu</i> (1979), and <i>Usami</i> (2001)	377
1923	<i>Hamada et al</i> (2001), and <i>Takemura & Moroi</i> (2002)	1187
1924 - 1925	<i>Utsu</i> (1979), and <i>Usami</i> (2001)	30
1926 - 2000	<i>JMA</i> (2002)	7243
1600 - 2000	Total	10416

Virtually the entire Kanto plain on which Tokyo sits has been subjected to $I_{JMA} \geq 6$, (equivalent to Modified Mercalli Intensity $MMI \geq IX$) shaking at least once since Edo (today's Tokyo) was first settled in 1603 (Figure 1a). Much of the strongest shaking is associated with three large shocks, the 1703 $M \sim 8.2$ Genroku, 1855 $M \sim 7.2$ Ansei-Edo, and 1923 $M = 7.9$ Kanto earthquakes (Figure 1b-d). The 1703 and 1923 shocks struck on the Sagami trough megathrust at shallow depth [*Nyst et al.*, 2006; *Shishikura et al.*, 2006], whereas the 1855 shock probably occurred beneath Chiba at much greater depth [*Bakun*, 2005; *Grunewald*, 2006] (Figure 1b-d). The peak intensity we report for the Kanto region is in substantial agreement with the compilation by *Miyazawa and Mori* [2005] for all of Japan.

INTENSITY DATABASE

The *Usami* [1994] and *JMA* [2004] catalogs span 82.5% of the time period, and thus form the backbone observations (Table 1). Unfortunately the observations from which *Utsu* [1979] drew intensity contour maps for earthquakes during 1885-1922 are unpublished and unavailable. Since most of the observations in the *Usami* and *Utsu* catalogs were referenced to the modern *JMA* scale (Table 2), we also use the *JMA* scale. On the basis of the observed frequency-intensity relationship that we will present in the next section, we judge the catalog to be clearly incomplete for $I_{JMA} < 3$ and possibly incomplete at $I_{JMA} = 3$, and so $I_{JMA} < 3$ data were excluded. Table 2 describes the principal felt effects and building damage employed to assess intensity. *Karim and Yamazaki* [2002] used a set of earthquakes with both intensity observations and strong ground motion records to deduce the peak ground acceleration (PGA) and peak ground velocity (PGV) associated with the *JMA* intensities; this equivalence

Table 2. Explanation of *JMA* seismic intensity scale and ground motion equivalents

Observations used to assess shaking intensity	<i>JMA</i> scale	Estimated Peak Ground Acceleration	Estimated Peak Ground Velocity	Estimated Seismic Intensity	Mercalli Int. <i>Richter</i> (1958)
Felt by most people in the building. Some people are frightened.	3	~ 0.02 g	~ 0.02 m/s	~ 0.02 m/s	~III-IV
Many people are frightened. Some people try to escape from danger. Most sleeping people awaken.	4	~ 0.07 g	~ 0.07 m/s	~ 0.07 m/s	~V-VI
Occasionally, less earthquake-resistant houses suffer damage to walls and pillars.	5 lower	~ 0.3 g	~ 0.3 m/s	~ 0.2 m/s	~VII-VIII
Occasionally, less earthquake-resistant houses suffer heavy damage to walls and pillars, and lean.	5 upper				
Occasionally, less earthquake-resistant houses collapse and even walls and pillars of highly earthquake-resistant houses are damaged.	6 lower	~ 0.9 g	~ 0.9 m/s	~ 0.8 m/s	~ IX-X
Many less earthquake-resistant houses collapse. In some cases, even walls and pillars of highly earthquake-resistant houses are heavily damaged.	6 upper				
Occasionally, even highly earthquake-resistant houses are severely damaged and lean.	7	~ 3.4 g	~ 3.3 m/s	~ 2.5 m/s	~ XI-XII
Source: <i>Japan Meteorological Agency</i> (2004)		Source: <i>Karim & Yamazaki</i> (2002)			<i>Shabestaria & Yamazaki</i> (2001)

makes the intensity data considerably more useful for engineering applications. Because intensities were historically measured in 1-2 story wood and masonry houses, they are principally sensitive to accelerations in the 5-8 Hz frequency range.

In 1996, JMA introduced a decimal seismic intensity scale calculated from acceleration records produced by seismic intensity meters calibrated to match the historical scale. Currently, JMA operates a network of 180 seismographs and 600 seismic intensity meters, and collects data from nearly 2,800 seismic intensity meters operated by local governments. We use the JMA intensity meter data, rounded to the JMA scale divisions shown in Table 2, in our observations.

We are making the complete data available online in both GIS and text formats at <http://earthquake.usgs.gov/research/modeling/intensities/> (*to be posted upon publication*)

MODERN AND HISTORICAL PERIODS

We divided our catalog into the historical period covering AD 1600 to 1925, drawn largely from *Usami* [1994] and *Takemura* [2003], and the modern period covering 1926 to 2000, which is based on *JMA* [2004]. Although both periods contain spatially rich data, the observation abundance and completeness differ (Figure 2). Fortunately, the two periods furnish complementary data. The historical period includes large destructive earthquakes such as those in 1703, 1855 and 1923, but poorly samples low-intensity shaking (Table 1). Because the largest event to strike during the modern period is a swarm of several $M \geq 7$ earthquakes in 1938, the modern catalog includes few high intensities, but is rich in low-intensity observations.

METHODOLOGY

We carried out the analysis in a GIS (geographic information system) that is linked to a large spreadsheet. This permitted us to manipulate and plot maps of the 10,000 observations in 2,000 cells, to readily test different assumptions on the resulting probabilities, and to overlay this information with geologic, geographic, and population data.

DATA DIGITIZATION

Although the post-1926 JMA intensity catalog includes latitude and longitude information along with the intensity observations, observation locations for Usami and Utsu

historical catalogs are not sufficiently accurate to digitize. As shown in Figure 3, the maps from which we work show an intensity symbol beneath a location name. So, rather than digitize these maps, we cross-referenced the ancient location names with several modern and ancient maps to assign coordinates to the observations. We also converted the mapped intensity symbols into numerical values using Usami's descriptions. We assigned observations in the Usami maps described as intensity ranges such as 'I_{JMA} 5 to 6' to I_{JMA}=5.5; 'I_{JMA} 5 or larger' was converted to I_{JMA}=5.25.

We followed a similar approach for Utsu observations for 1885-1925. I_{JMA}≥3 intensities reported by *Usami* [2001] were digitized as previously described, but for most earthquakes during this time period, we have only interpolated intensity contours [*Utsu*, 1979; *Utsu*, 1982; *Utsu*, 1988; *Usami* 2001]. So we digitized the contours at sites where we also have JMA intensity data for the 1923 Kanto earthquake. Thus the natural variability and inconsistency of the observations is lost. Fortunately, few large earthquakes struck during this period, and the 1923 JMA site coverage was sparse. So at worst, we under-sample intensities during 1885-1925.

We use three data sources for the 1923 Kanto earthquake and the first three months of aftershocks. The digital JMA catalog intensities were directly imported to the GIS. The 1923 JMA catalog, however, includes little data where destruction was near total, such as along the Tokyo-Yokohama corridor. To fill this gap and enhance the spatial sampling, we also included an intensity map published by *Takemura* [2003]. Because the *Takemura* [2003] data were not made available to us in digital format, we digitized the center point of each township for which intensity was assigned (ranging from 2 x 2 to 10 x 15 km areas), including JMA stations where available. Finally, *Hamada et al.* [2001] published aftershock intensities recorded at all JMA and several other seismic observatories for the 3 months after the 1 September 1923 earthquake. The aftershock data have high temporal and low spatial sampling.

GRIDDING AND BUFFERING

We divided our study region into 5 x 5 km cells for mapping and statistical analysis. Cell size trades off observation density with spatial coverage. We chose a cell size to capture the scale of geologic features that influence site amplification, such as the width of streambeds and the extent of soft sediments that rim Tokyo bay. Further, the bias created by the much

more densely sampled 1923 and 1854 earthquakes is minimized, as multiple observations in each cell are averaged. Although intensity observations are stored as points, they represent shaking recorded in a town or village. Thus, to smooth the data, we applied a radius buffer of half the cell width, or 2.5 km, to each observation point (Figure 4). This method also helped us to minimize location uncertainty of historic observations. As shown in Figure 4, the buffering causes stations near cell borders to influence adjacent cells, and so the total number of cells with data increases.

REGIONAL FREQUENCY-INTENSITY CURVE

We combine observations from all cells to find a regional frequency-intensity distribution. This is similar to calculating a b -value from a frequency-magnitude distribution, with intensity replacing magnitude. As shown in Figures 2 and 5a, the modern portion of the catalog has few $I_{JMA} \geq 6$ observations simply because there have been few large earthquakes in the area during this period; the historical portion is incomplete for $I_{JMA} \leq 5$ due to incompleteness at low intensities. We have excluded the incomplete data in historical catalog and merged the remainder.

The data are well fit by an exponential decay curve (Figure 5b). Although a power-law curve might be expected for the attenuation of strong ground motion with distance, intensity assignments are based on damage descriptions and thus are not strictly scaled numerically, and so the relation need not be power-law.

There are two reasons for such an observed decay relation, earthquake abundance and seismic attenuation: First, similar to a b -value plot, there are many more small earthquakes than large ones. Second, there are many more epicenters far from a given observation station than close to it. Thus, observations of weak shaking are far more common than strong shaking. In Figure 5c, we assume a b -value of 1.0, as found for the Kanto region by *Grunewald* [2006]. Next, we randomly distribute 1 million $5 \leq M \leq 8$ earthquake sources over the Kanto area, extracting 400-yr periods by Monte Carlo simulation. Finally, we use the intensity attenuation relations developed for the Kanto region by *Bakun* [2005]. The resulting theoretical frequency-intensity relations are in close agreement with the observations, particularly if most earthquakes locate in the crust.

APPLYING REGIONAL SLOPE TO LOCAL CELLS

We assume that the regional decay slope applies to each individual cell, but allow the intercept to vary in each cell. In other words, the ratio of strong to weak shaking is assumed constant, but the frequency of shaking is permitted to vary. Because we are only solving for the intercept (or frequency), this permits us to calculate earthquake probabilities for cells that contain only a few observations. This approach is consistent with independent observations that the spatial variability of b -values is smaller than variations in earthquake rate [Wiemer and Wyss, 1997]. In Figure 6, we test how well the exponential decay curve satisfies the observations for eight cities with cells containing a large number ($n=50-400$) of observations, and for two cities with a small number ($n=4-8$). Regression coefficients (R^2) for the six cells with plentiful observations range from 0.88-0.99, and the least squares (Π) misfit ranges from 0.17-0.01, indicative of good fits to the observations. Yokohama, with 256 observations, yields nearly the same probability as West Yokohama, with only 8 observations 15 km away.

CELL RELIABILITY

Significant portions of the Kanto area lack intensity observations. In addition, there are numerous cells with sparse data that do not fit the curves; an example, Gotemba, is shown in Figure 6b. We experimented with interpolation between reliable cells, but found that this tended to exaggerate areas of strong shaking. So we chose instead to omit cells without intensity observations, and to distinguish less reliable cells in the maps. Although this markedly reduces the area of coverage, we have observations wherever there is population (compare Figures 7b and 7d), and for the most part, this is where the earthquake hazard is most important.

Cell reliability is assessed by the least squares fit to the model (Figure 7a), the number of observations (Figure 7b), and the time period covered (Figure 7c). This information is combined in the criteria to identify reliable cells:

Data abundance criteria: Number of observations ≥ 50 or number of intensity levels ≥ 3 and number of $I_{JMA}=5 \geq (I=6 + I=7)$

or

Data consistency criteria: Least squares < 0.1 and $R^2 > 0.8$ and number of I_{JMA} observations $=5 \geq (I=6 + I=7)$ and number of observations ≥ 2 and time period ≥ 10 yr

RESULTS

DISTRIBUTION OF SHAKING PROBABILITY

The frequency f of any JMA intensity can be transformed into a Poisson or time-averaged probability P for any time-period t by $P=1-\exp(-ft)$. We use $I_{JMA}=6$ because it represents severe shaking and is well sampled by the data. The resulting 30-year probability of severe shaking is ~35% in the Tokyo-Kawasaki-Yokohama corridor, ~30% in Tateyama, ~15% in Choshi, and ~15% in Kumagaya (Figure 8a and Figure 8b).

COMPARING OUR RESULTS TO GEOLOGY

Perhaps the strongest test of our results is whether the distribution of probability reflects the surficial geology and distribution of major faults (Figure 8c), since neither geology nor faults were imposed on the results or used in the calculations. In fact, we find a correlation between the probability and the presence or absence of stream deposits and bay mud, and between probability and proximity to the plate boundary faults, which are the sources of the largest earthquakes (compare Figures 8a with 8b). To minimize sensitivity to outliers in the correlation, we consider all cells with probabilities $\leq 45\%$ and distances from the major faults ≤ 150 km. A linear distance-dependence accounting for 24% of the variance is found such that the probability at major faults the probability is 16% and 150 km away it is 6%. The mean shaking probability of cells in soft sediments is 19% and for bedrock it is 14%.

TEST OF KEY ASSUMPTIONS

IS THE CATALOG TYPICAL OF LONG-TERM BEHAVIOR?

To use the observed record of shaking to estimate typical behavior, we must assess whether the 400-year period of intensity observations is sufficiently long. From the geodetically measured strain and vertical deformation during the past 15 years, *Nishimura and Sagiya* [2006] inferred the seismic moment accumulation rate (the product of the cumulative fault slip rate, fault area, and crustal stiffness). *Grunewald* [2006] estimated the magnitude, location, and uncertainty of historical earthquakes since 1600, and performed a Monte Carlo simulation of the likely moment release rate associated with these earthquakes. *Grunewald* [2006] found the seismic release rate to be in close agreement with the moment accumulation rate. This means that the catalog is likely representative of the long-term

process. Further, *Shishikura* [2003] and *Shishikura* [in prep.] developed a record of 16 Sagami plate boundary earthquakes during the past 7200 years from uplifted marine terraces along the Boso peninsula, and *Stein et al.* [2006] used this record to infer a 403 ± 66 yr mean interevent time for $M \geq 7.9$ events, about the time period of our intensity catalog. Thus, both analyses support our reliance on the 400-year catalog: the moment accumulation and release rates are in balance, suggesting this period includes neither an earthquake deficit nor oversupply; and the catalog duration is roughly equal to the observed plate-boundary earthquake cycle, implying that the record likely encompasses the typical range of seismic behavior.

ARE THE INTENSITY DATA BIASED WITH TIME?

The second issue is whether there are systematic changes in the intensity standards because the observation density and spatial coverage increase with time, and because the building stock from which intensities are inferred changes with time. The best way to test this is to compare the intensities for two earthquakes of the same size and location that occurred centuries apart. Tsunami and marine terrace uplift data [*Shishikura*, 2005] indicate that the 1923 Kanto and 1703 Genroku both slipped the two westernmost fault patches by the same amount; the difference between the events is that the 1703 shock slipped two additional patches to the east (compare Figures 1b and 1d). In Figures 9a-b we show the subset of cells with intensity observations for both events. Their resemblance is quite evident; the mean difference in intensity for these cells between 1703 and 1923 is only 0.26 Intensity units. When comparing events with the same source, path, and site effects, attenuation equation (8) of *Bakun* [2005] for the Kanto area subduction events reduces from

$$I_{\text{PRED}} = -8.33 + (2.19 \pm 0.32)M_{\text{JMA}} - 0.00550 \Delta h - 1.14 \log \Delta h$$

to $dM_{\text{JMA}} = dI_{\text{JMA}} / (2.19 \pm 0.32)$, where dM_{JMA} is the difference between the two earthquake magnitudes, dI_{JMA} is the difference between the mean intensities, and Δh is in km. This results in an apparent JMA magnitude difference of 0.1 units for the 1703 versus 1923 earthquakes, in substantial agreement. Thus for the 200-year time span, intensities appear comparable, a testament to the work of Usami and Takemura.

We can also compare the 1855 $M \sim 7.2$ Ansei Edo earthquake intensities to that of the 23 July 2005 $M = 6.0$ Chiba shock that produced an intensity distribution similar to 1855 [*Grunewald*, 2006], but with proportionally smaller values (Figures 9c-d). This similarity

also argues that the past 150 years of intensities are comparable. The slope of the regression of all cells with both 1855 and 2005 observations is 0.7 (perfect agreement would yield 1.0), and the mean difference in intensities is 1.32 (in other words, a site with an intensity of 6 for 1855 corresponds to an intensity just below 5 in 2005). If we assume that the earthquakes share the same hypocenter, then using equation (8) from *Bakun* [2005] for crustal earthquakes, $dM_{JMA}=dI_{JMA}/2.19$, and $dM_{JMA}=0.6\pm0.1$. So for 1855 Ansei-Edo, $M_{JMA}=6.6\pm0.1$. By comparison, *Usami* [2003] found $M=7.1$, *Bakun* [2005] found $M=7.2$, and *Grunewald* [2006] found $M=7.4$.

ARE RESULTS TOO SENSITIVE TO KEY EARTHQUAKES?

The 1923 Kanto and 1855 Ansei Edo earthquakes exert the largest influence on the probability maps. *Stein et al* [2006] estimate an inter-event time of 403 ± 66 yr for the Kanto earthquake and a more uncertain ~ 150 yr for the Ansei-Edo earthquake, and so such events might be expected in a 400-year-long catalog drawn at random.

The 1703 Genroku earthquake is more infrequent, with a ~ 2200 -year interevent time [*Shishikura*, 2003], but because of the paucity of 1703 intensity observations, it only modestly influences the probabilities. The Nagano region near the northwest corner of the map sustained the destructive 1847 Zenkoji $M\sim 7.4$ earthquake, which killed 8,000 people. An 1858 $M\sim 7.0$ earthquake also struck just outside of the western map boarder. Paleoseismic evidence suggests that the Nagano-Bonchi-Seien fault that ruptured in the 1847 earthquake has 800-2500-year interevent time [*Earthquake Research Committee*, 2005], and so the 1847 event would not be typical of a 400-year catalog. We thus repeated our analysis excluding intensity observations for the 1703 and 1847 earthquakes. When excluded, the JMA $I\geq 6$ probability decreased 7% at Nagano, 6% at Yokohama, 4% at Kofu, and 3% at Tokyo, and 1% Kumagaya (Table 3). Thus our results are modestly sensitive to these two earthquakes.

Table 3. Probability of $I_{JMA} \geq 6$ shaking ($PGA \geq 0.9g$) in key cities

Site name	Cell id	Longitude	Latitude	Number of observations	30-year Poisson probability (%)	
					Using all data	1703 & 1847 Eqs. removed
Tokyo	5666	139.76825	35.70035	354	38	35
SW Tokyo	5587	139.72333	35.66371	353	36	31
Yokohama	5118	139.67841	35.44348	265	30	14
Nagano	7737	138.19619	36.68335	275	23	16
Kumagaya	6593	139.36400	36.13878	208	14	13
Kofu	5561	138.55552	35.66371	145	22	18
Choshi	5768	140.84622	35.73698	271	17	14
Tateyama	4186	139.85808	35.00119	139	21	14
West Yokohama	5115	139.54367	35.44348	8	25	15
Gotemba	4789	138.91485	35.29632	4	7	5

DISCUSSION

COMPARISON TO OTHER STUDIES

Stein et al. [2006] analyzed the earthquake probability for Tokyo by relocating the historical earthquake catalog, associating earthquakes with faults, inferring the seismic slip rate of the fault sources, and estimating the inter-event time for the largest earthquakes. They found a 29% probability of earthquakes capable of producing JMA $I \geq 6$ shaking in the Tokyo-Yokohama corridor, in good agreement with our findings here. The Japanese government issued a comprehensive study of the earthquake and shaking likelihood for all of Japan [*Earthquake Research Committee*, 2005], publishing a map showing the time-dependent 30-year probability of JMA $I \geq 6$ shaking for greater Tokyo (Figure 10). Because the digital files have not been published, we re-plotted the Tokyo portion of our map in the same probability color scale as that of the Earthquake Research Committee. Some 59% of the cells in both plots have the same probability level, and 98% are within one probability level. Thus, despite the large differences in approach, the probabilities are similar for Tokyo and its surrounding cities.

USE OF OUR RESULTS FOR BUILDING CODE REGULATIONS

Regulators of building construction standards often base their codes on the level of shaking for which there is a 10% chance of exceeding in 50 years, roughly equivalent to the

maximum shaking that might be observed in a 500-year period. We make such an exceedance calculation in Figure 11a, which can be compared with the peak shaking observed during the past 400 years (Figure 1a). Not surprisingly, the two maps are similar. There is more detail in the exceedance map because it is incremented in decimal JMA intensities, and because the exceedance map uses all observed intensities, whereas Figure 1a uses only the small subset of maximum observed intensities. In Figure 11b, the exceedance map is presented in units of peak ground acceleration (PGA), using the empirical relations of *Karim and Yamazaki* [2002]. Given the nature of intensity observations on 1-3 story buildings, this map is most valid in the frequency range of 5-8 Hz.

USE OF OUR RESULTS FOR CATASTROPHE BONDS

Global reinsurance companies reduce their financial exposure by spreading risk among policies in many countries, and by transferring some risk to the much larger capital markets by issuing insurance-linked securities, known as catastrophe bonds. These bonds pay a high rate of quarterly interest unless the specified catastrophe occurs, in which case the investor could lose his or her principal. An earthquake catastrophe bond could be ‘triggered’ by, among other things, an earthquake of a given magnitude falling into a specified location, or by shaking exceeding a specified threshold. Such bonds typically have maturities of less than a decade, and the investor must be able to assess the benefit of the high interest rate against the risk of losing the principal. Figure 12 shows a calculation for a hypothetical bond with a 5-year maturity. There is a 5% chance of a $M \geq 7.2$ shock striking somewhere within the box, a magnitude that *Stein et al.* [2006] associate with JMA $I=6$ (PGA ~ 0.9 g) shaking. If the trigger were instead $\text{PGA} \geq 0.9$ g shaking at a specific city, there is a 7% chance in central Tokyo, and an 8% chance in Yokohama.

APPLICATION OF THIS METHOD ELSEWHERE

At first glance, one might conclude that intensity-based probability modeling that we have presented is restricted to areas such as Japan that possess long histories of frequent large earthquakes, but we suspect that this is not so. The sole requirements are a high spatial and temporal density of observations. In Italy, there are 35,000 observations recorded at 12,000 sites for 600 earthquakes for the period BC 461-AD 1997. Equally important, there are 15 sites in Italy with more than 50 observations. So, despite a much lower rate of seismicity, Italy possesses three times Japan’s number of observations. This is because in countries that

rarely experience large earthquakes, people tend to report many more observations of small shocks. Because in our method, the distribution of low intensities can be used to project the expected frequency of high intensities, a high rate of large earthquakes is not essential. Other sites amenable to such an analysis include France (18,000 intensity observations of 33 earthquakes for the period 1866-2003) and perhaps even California (52,000 $\text{MMI} \geq 3$ observations of 7,900 earthquakes for the period 1769 to 1985).

CONCLUSIONS

The premise of this study is that if one would like to estimate the likelihood of shaking, then using past shaking observations furnishes a direct and perhaps reliable answer. The principal benefits of this approach is that it builds the fewest possible assumptions into a probabilistic seismic forecast, and that it includes site and source effects without imposing this behavior. The cost is that we must abandon any attempt to make a time-dependent forecast (describing the likelihood during the next 30 years, rather than during an average 30 years), which could be quite different. We believe the method is suitable to many applications of probabilistic seismic hazard assessment, and can be successfully applied to other countries and regions. At the very least, we view this data-rich method as an alternative that can be compared to assumption-rich approaches. In the Kanto region of Japan, the results are roughly equivalent to conventional seismic hazard analysis, and so encouraging.

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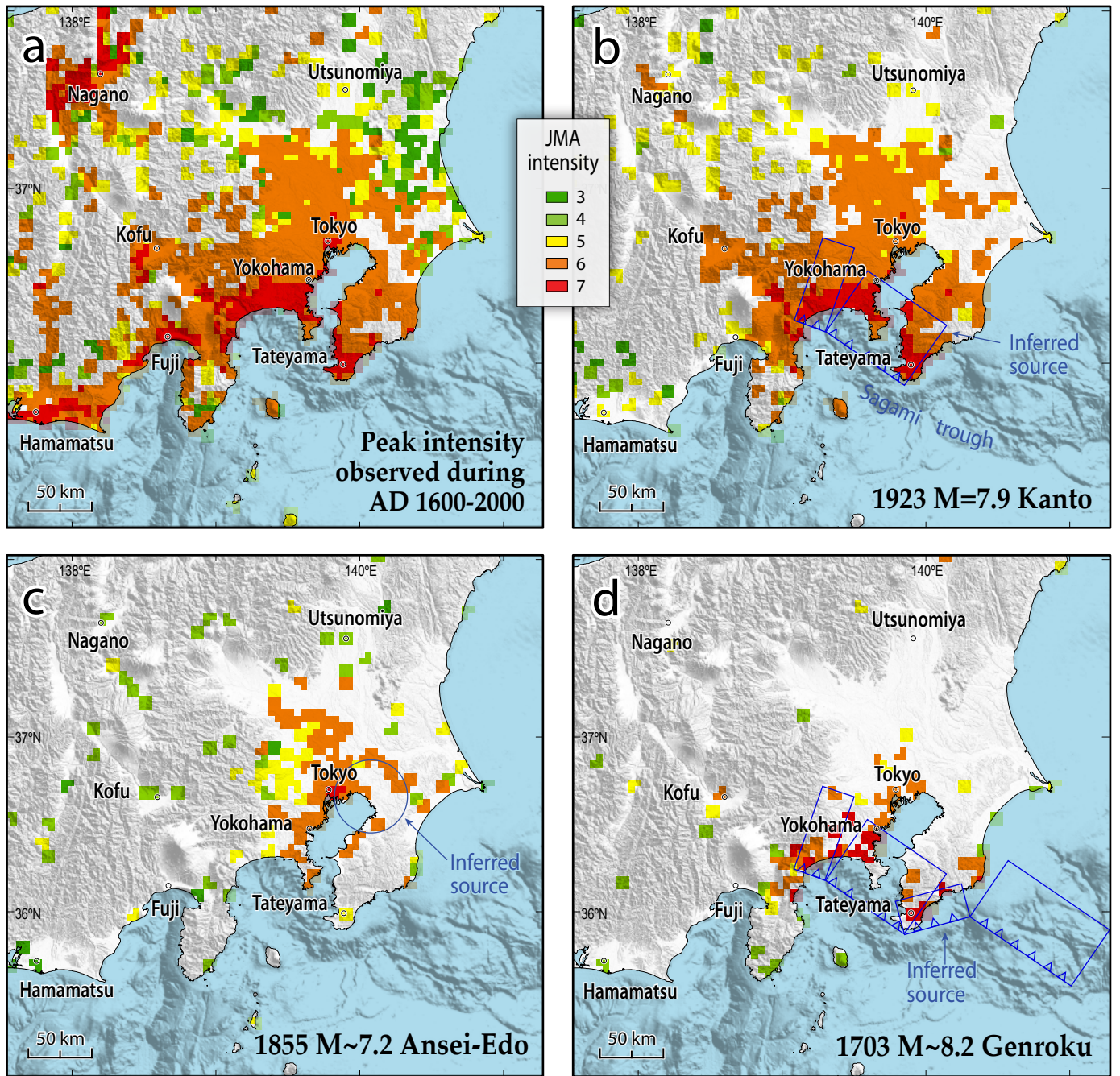


Figure 1. Maps of earthquake intensities observed within 5 x 5 km cells. (a) Peak intensity for the entire catalog duration. (b-d) Intensity distribution for the three largest earthquakes recorded during the 400-year period, with sources inferred by Nyst *et al* [2006] for 1923, Grunewald [2006] for 1855, and Shishikura *et al* [in prep.] for 1703.

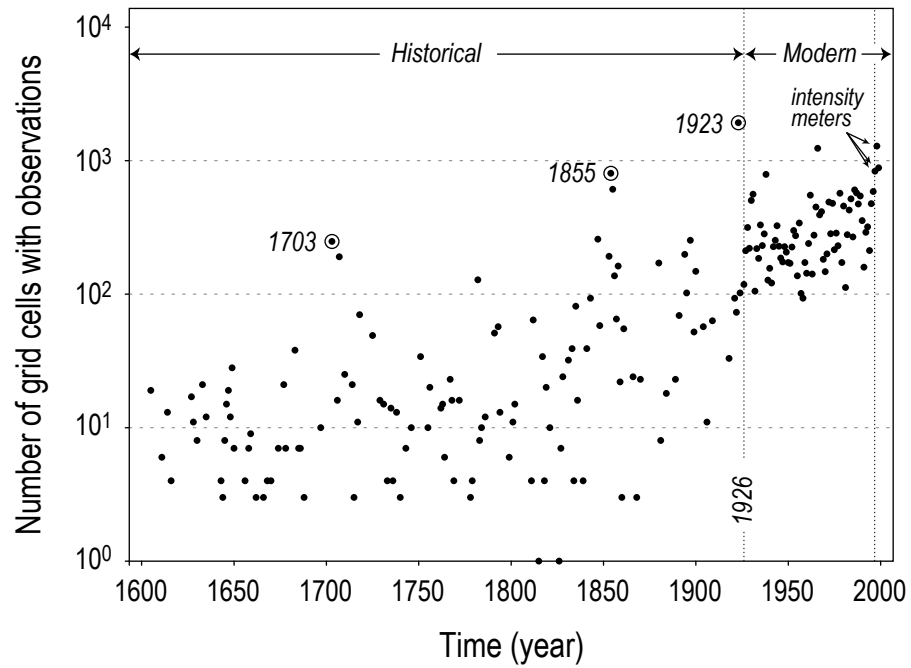


Figure 2. The long-term increase in the number of cells with intensity observations and the large number of cells for the three largest earthquakes are evident. After 1926, the JMA systematically recorded earthquake intensities.

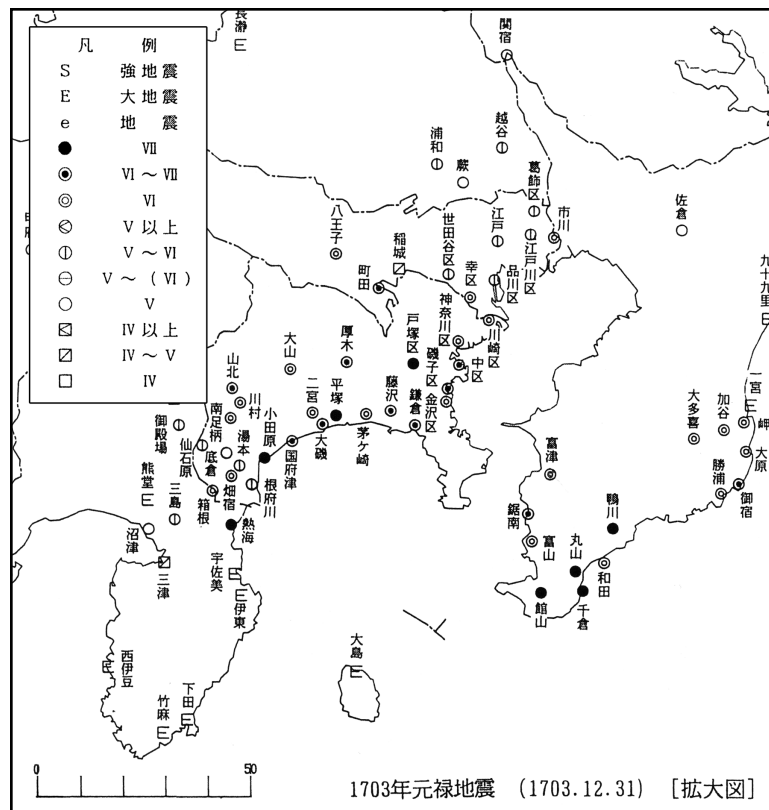


Figure 3. An example of an earthquake intensity map from *Usami* [2003], for the 1703 M~8.2 Genroku earthquake. The symbols depict intensity levels, the characters above the symbols denote town names.

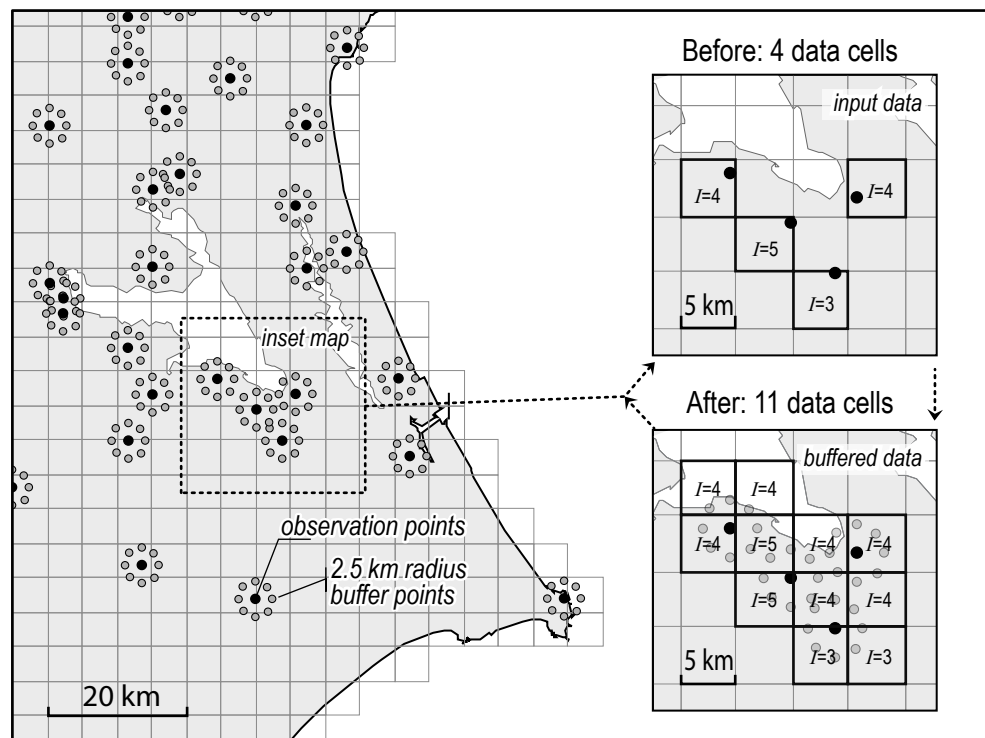


Figure 4. Intensity observations (black dots) are buffered, a form of smoothing (gray dots) so that more cells (squares) contain observations, making the resulting cell intensities less sensitive to location errors.

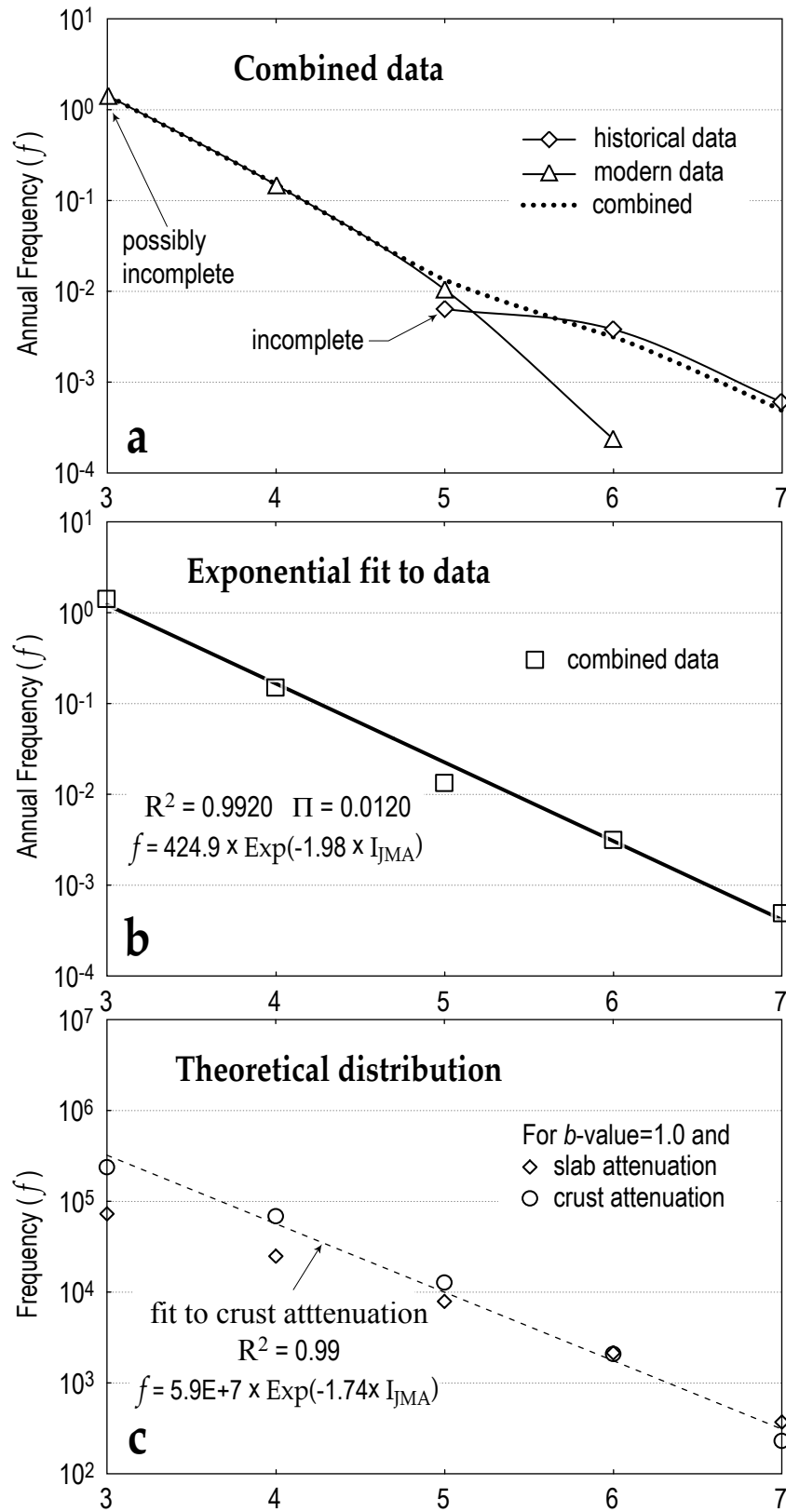
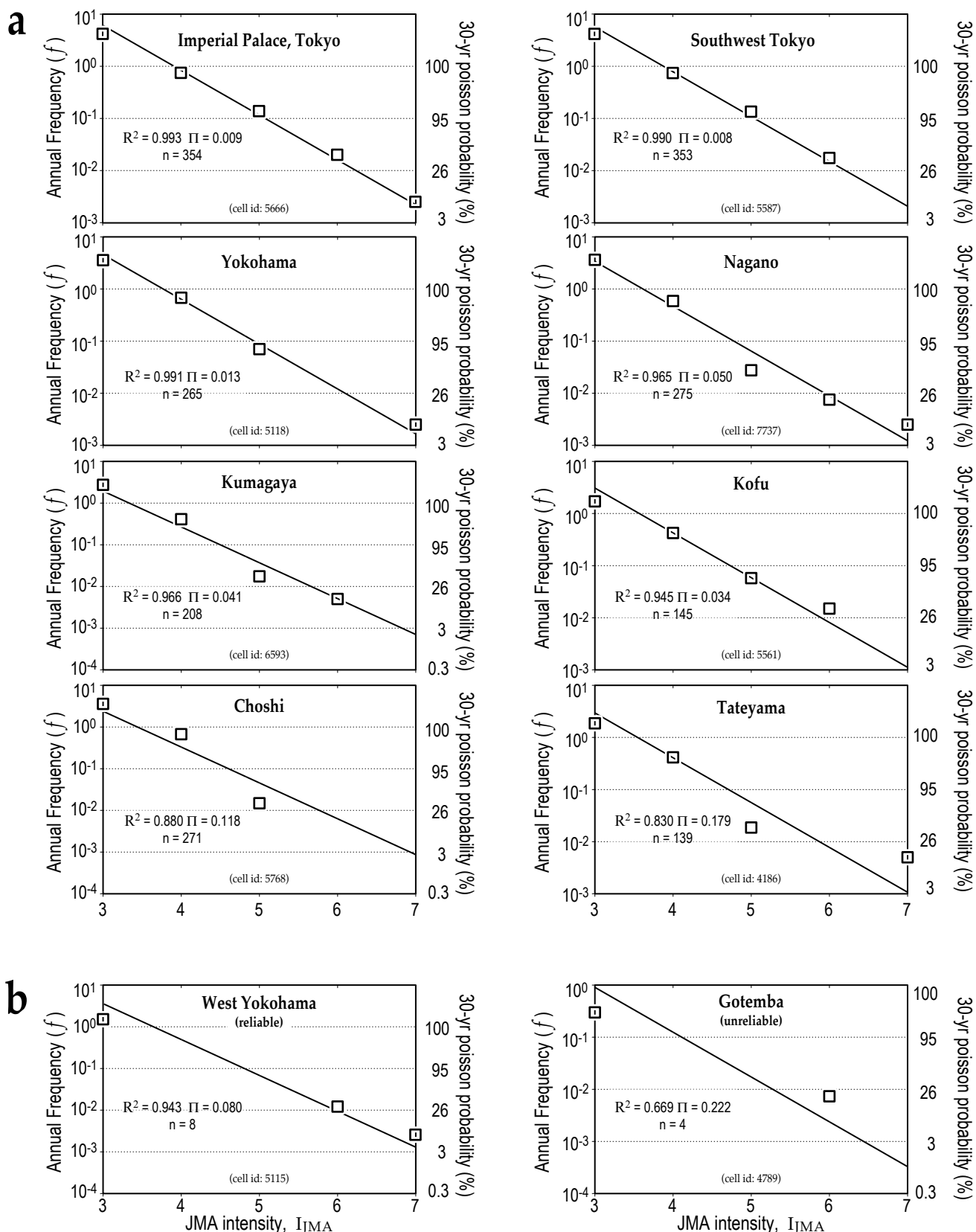


Figure 5. Frequency-intensity relation for the 10,416 combined observations, resembling the more familiar b -value (frequency-magnitude) relation. (a) Historical and modern data from Figure 2 are combined. (b) Fit of data to an exponential curve. (c) Theoretical distribution assuming a b -value of 1.0, a random distribution of $5 \leq M \leq 8$ earthquakes, and the Kanto regional attenuation relations for subduction slab and crustal earthquakes of *Bakun* [2005].



Legend: R^2 = Regression coefficient Π = Least squares residual n = Number of observations

Figure 6. (a) Fit of the observations for 8 cities to the regional slope, with only intercept determined locally; the regional slope found in Figure 5 is seen to fit the local data well. (b) West Yokohama and Gotemba are examples of cells with few observations; the former is deemed reliable and the latter unreliable.

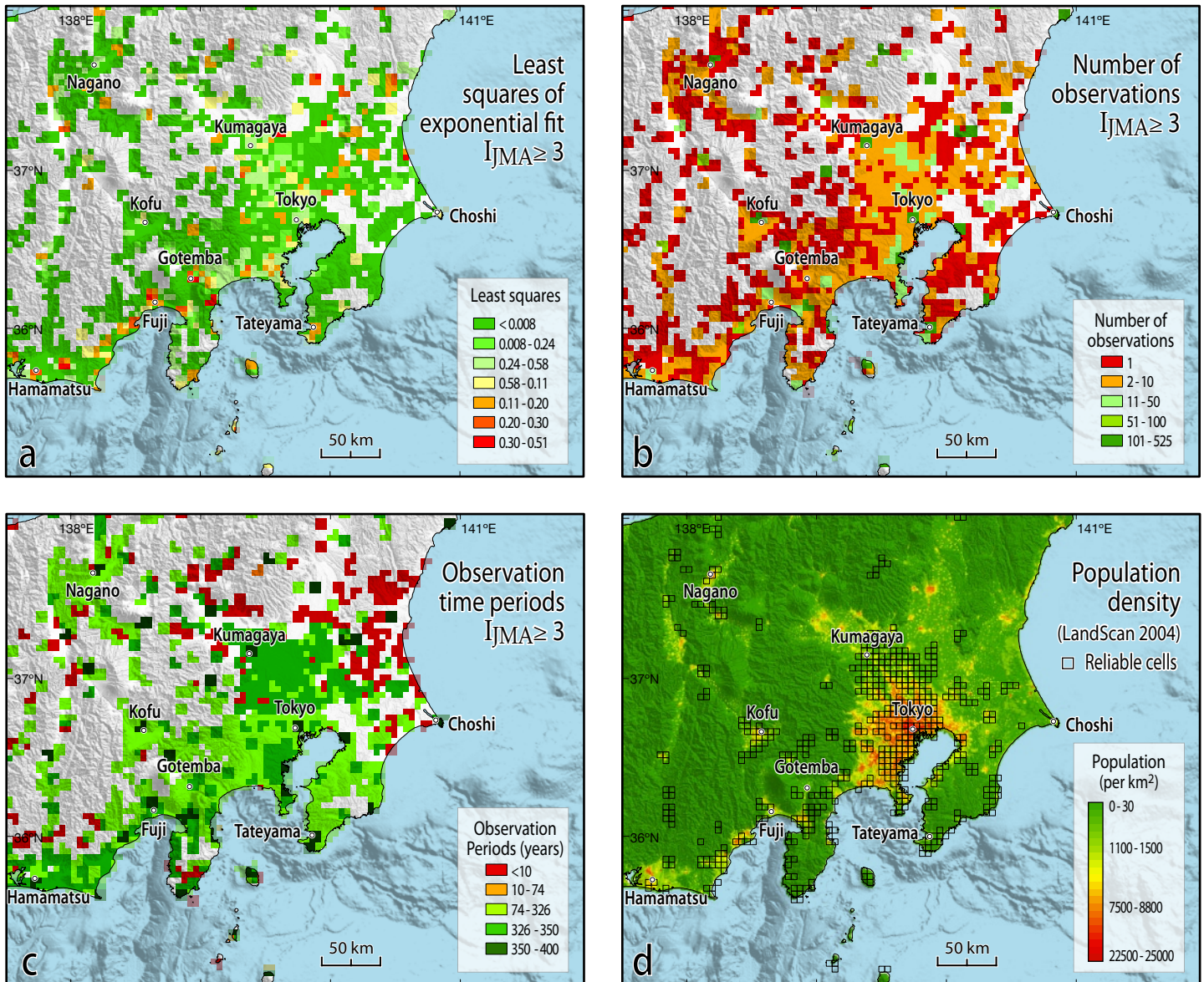


Figure 7. Three criteria used to evaluate cell reliability. (a) Least squares residuals to the exponential fit. (b) The number of intensity observations. (c) The time period of the observations. (d) Cell coverage reflects the spatial distribution of population. Although we lack uniform coverage, coverage is concentrated where people live.

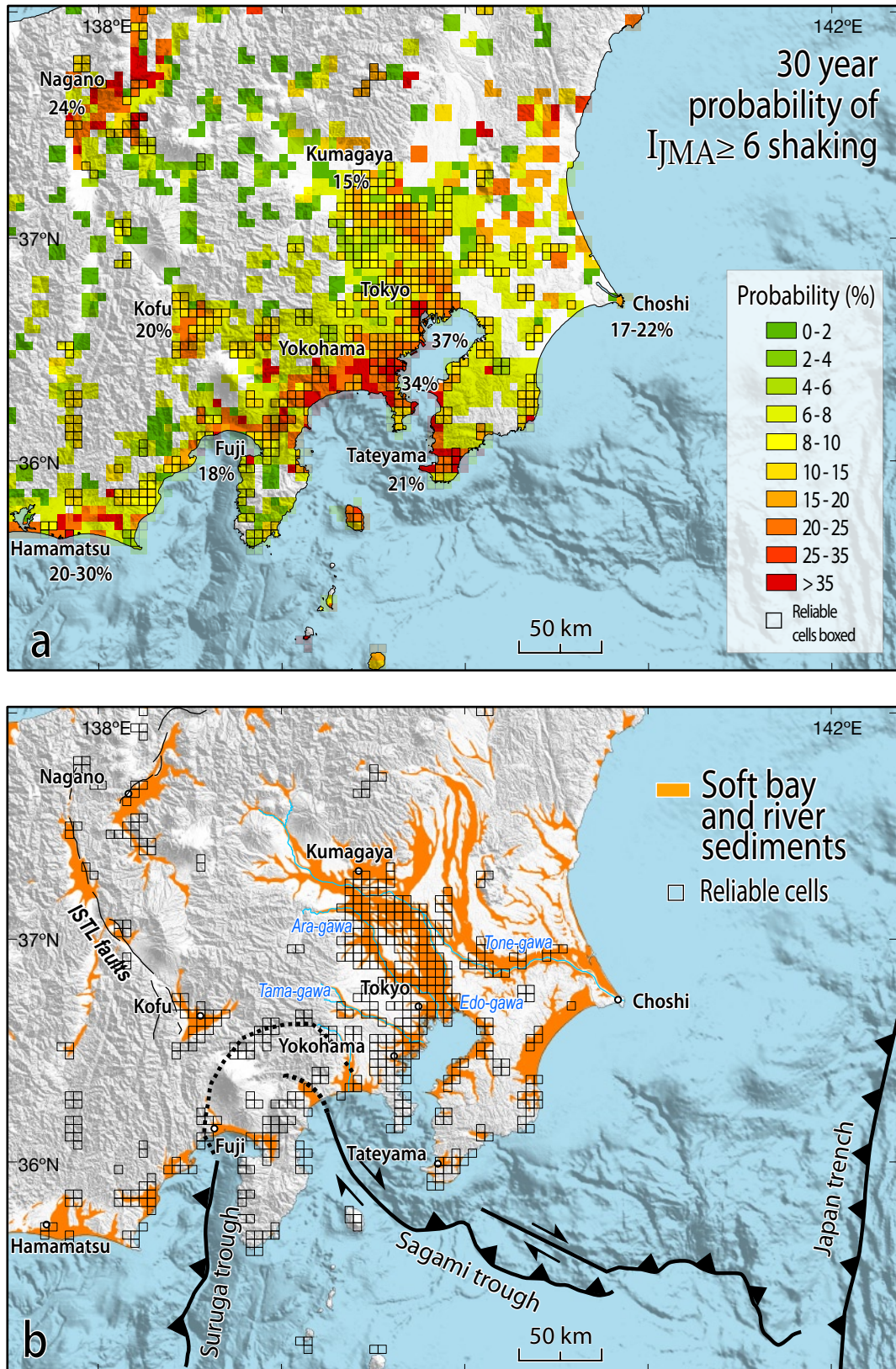


Figure 8. (a) The 30-year probability of JMA $I_{JMA} \geq 6$ shaking (equivalent to $\text{MMI} \geq \text{IX}$). Tokyo, Yokohama and Nagano span multiple grid cells, and so percentages shown average cells for those cities. (b) The shaking probability is higher in river sediments and bay mud; and the probability increases with proximity to the major faults.

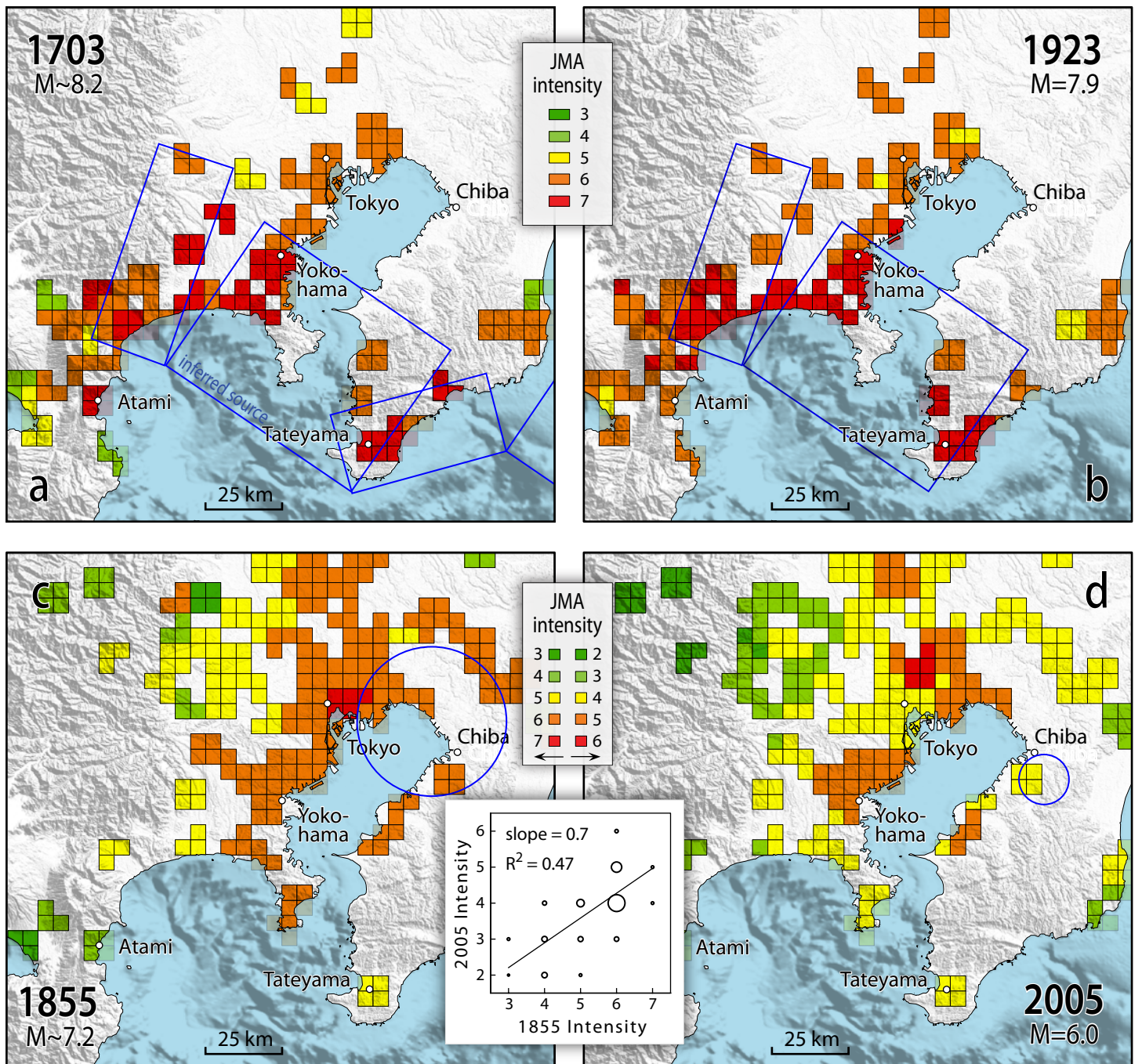


Figure 9. To assess systematic shifts in the intensity scale with time, we compare intensities for cells with observations from two earthquakes that struck 150-200 years apart. Intensities are plotted in the near-source region that contains 70% of the common observations. (a) 1703 M~8.2 Genroku earthquake intensities compared with (b) 1923 M=7.9 Kanto earthquake intensities. The mean difference in intensity is 0.26 intensity units, corresponding to 0.1 magnitude units. (c) 1855 Ansei-Edo earthquake intensities compared with (d) 2005 M=6.0 Chiba earthquake intensities. A regression on their intensities is inset (circle size is proportional to number of observations), with a slope close to 1.

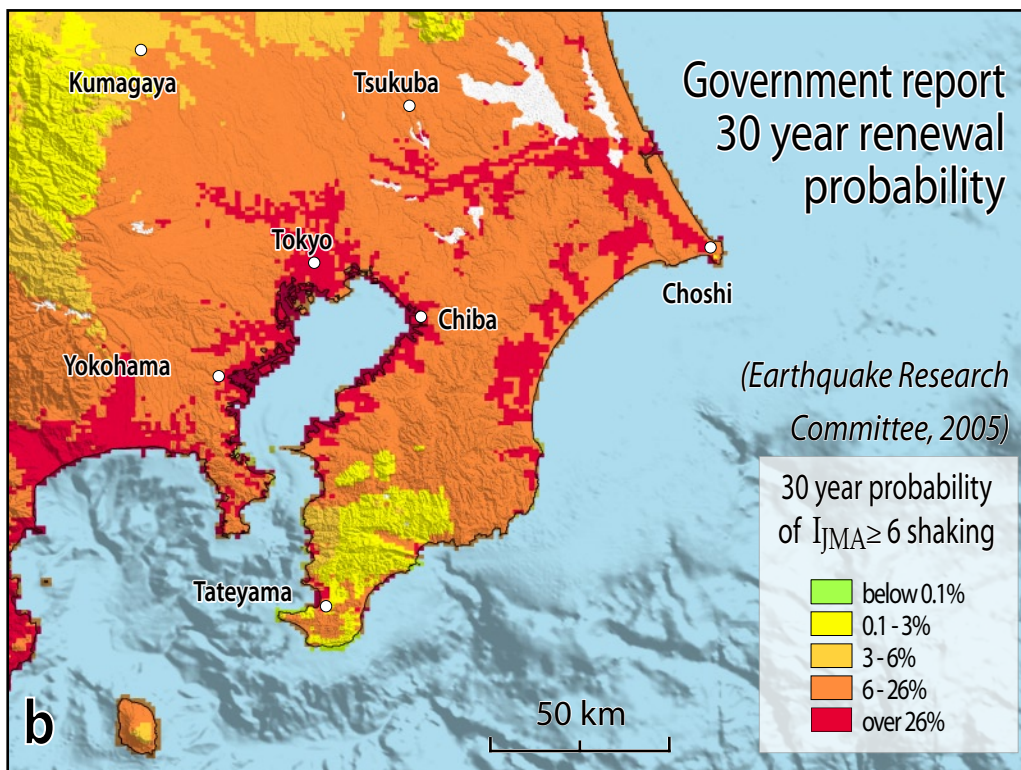
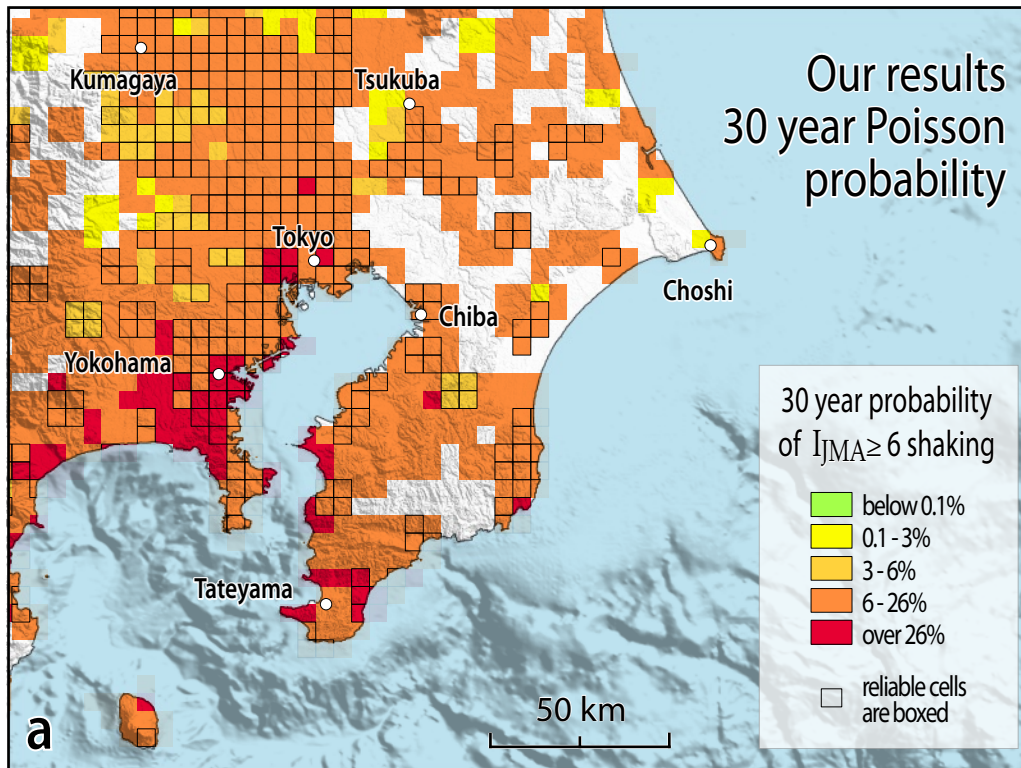


Figure 10. Using the probability scale adopted by *Earthquake Research Committee* [2005], we re-plot our results for the immediate vicinity of Tokyo; results are similar for this region despite different approaches.

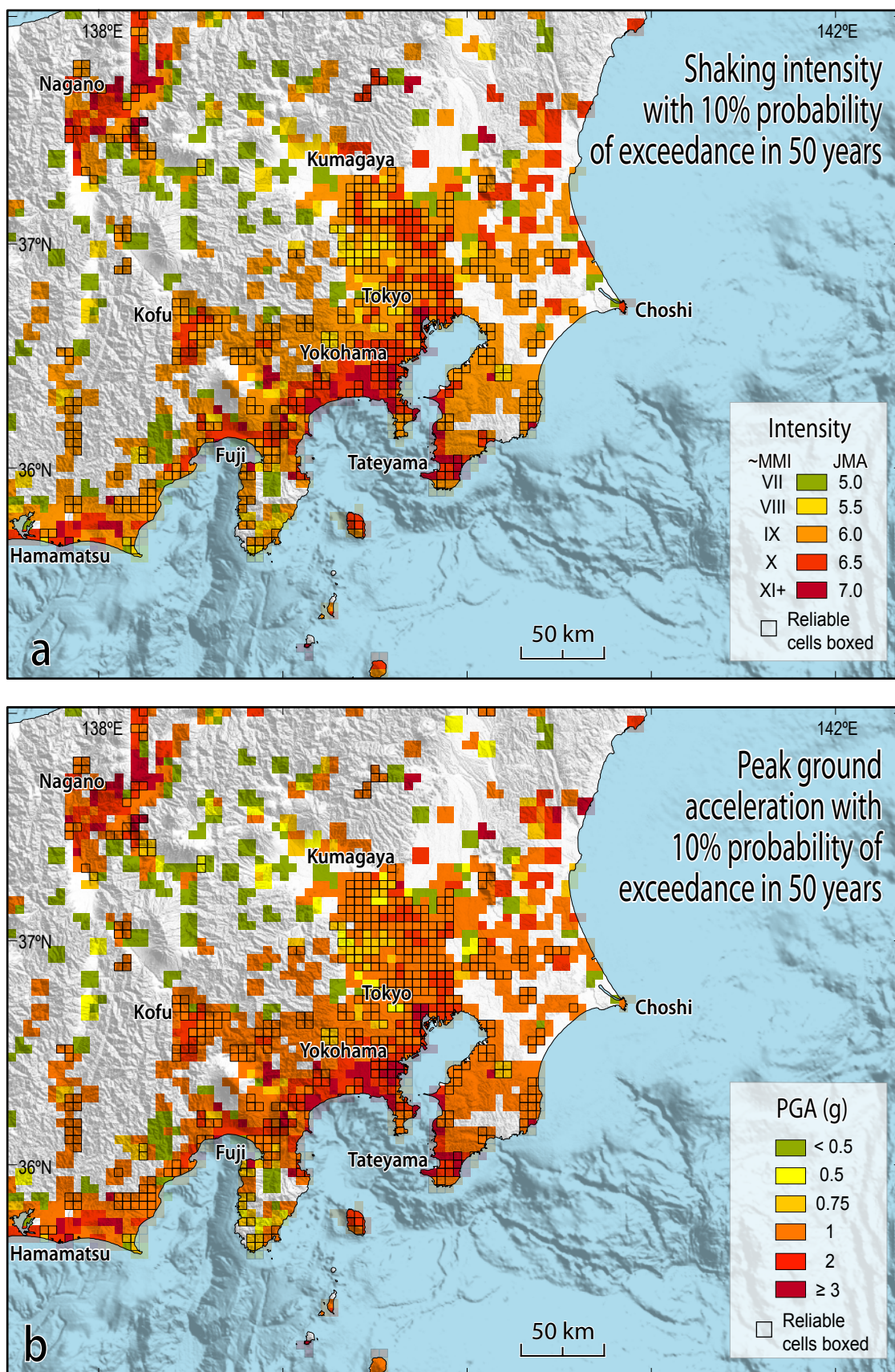


Figure 11. Map of the JMA intensity (a) and PGA shaking (b) for which there is a 10% chance of exceeding in an average 50-year period, a criteria often used by building code regulators. In (a), both JMA and MMI intensities are shown. In (b), the accelerations are most indicative of 5-8 Hz frequencies characteristic of 1-3 story buildings used to assess the intensities.

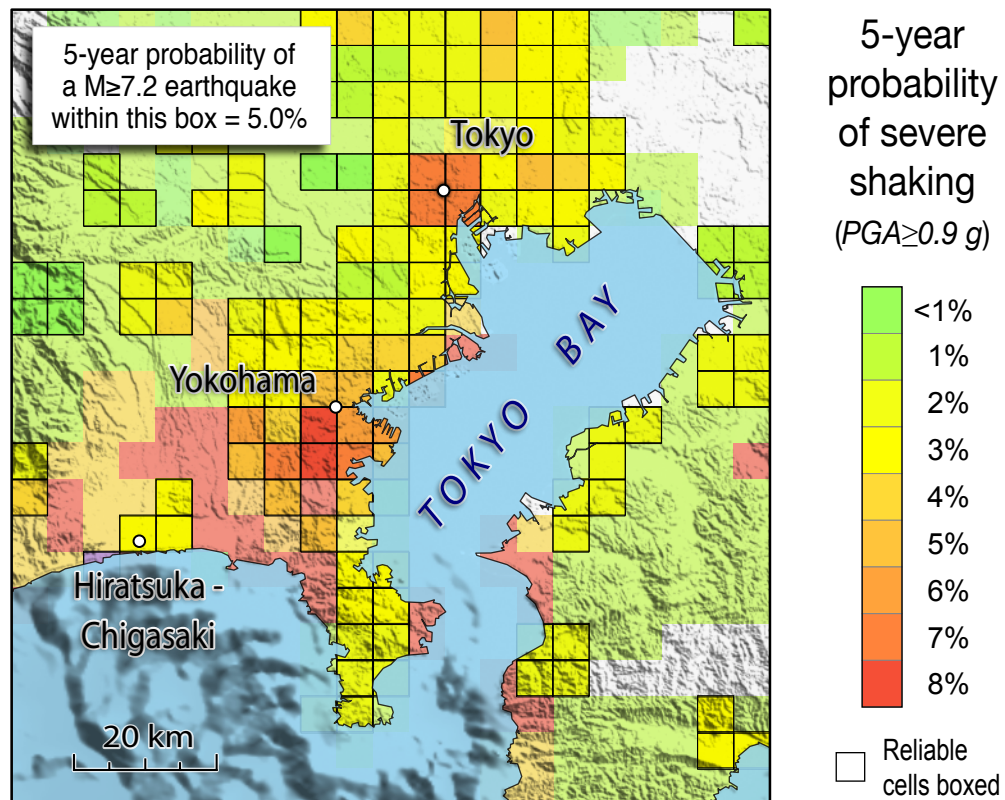


Figure 12. An illustration of a hypothetical catastrophe bond triggered by an earthquake of a given size and location (here, a $M \geq 7.2$ shock within the box), or by a specified level of observed shaking. The bond could be triggered by shaking in a restricted 5 x 5 km site, such as Tokyo Disneyland or the port of Yokohama, or it could be a regional average.